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To be published in the Astrophysical Journ ...

DISTRIBUTION STATEMENT A

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Supported by NASA Grant NGL 05-020-272 NASA Contract NASA 8-37334 ONR Contract N00014-85-K-0111

# A 154-DAY PERIODICITY IN THE OCCURRENCE RATE OF PROTON FLARES

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#### ABSTRACT

We have analyzed periodicities in the occurrence rate of proton flares for solar cycles 19 through 21 (1955-86) and have identified two epochs that exhibit a 154-day periodicity. These epochs are a 14-year interval from 1958 January through 1971 December and a 5.5-year interval from 1978 February to 1983 August. The best-determined period is 154.6(±0.6) days. We have found that the phase of this periodicity changed between the abovementioned two epochs by about one half of a period  $(\Delta \phi = 0.5 \pm 0.16)$ . It appears that the occurrence rate of proton flares is more sensitive to the 154-day periodicity than the occurrence rate of flares selected by other criteria. Keywords:

> Solar Activity Surspots Ac-rophysics, Periodic Variotions,

> Proton Flares, Sun,

NTIS CRAM DTIC Unannounced

> STATEMENT "A" per Dr. N. Sheeley NRL/Code 4172 TELECON 3/19/90

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#### I. INTRODUCTION

A periodicity of about 154 days was discovered by Rieger et al. (1984) in the occurrence rate of gamma-ray flares detected by the Gamma-Ray Spectrometer aboard the Solar Maximum Mission (SMM). They also found the same periodicity in the occurrence rate of flares with a soft X-ray classification above M4. This periodicity was confirmed by Kiplinger et al. (1984) who analyzed flares detected by the Hard X-Ray Burst Spectrometer aboard SMM, and has subsequently been found in the occurrence rates of flares selected by various observational criteria: microwave flux (Bogart and Bai 1985), Hα importance (Ichimoto et al. 1985), Hα flare index (Ozguc and Atac 1989), and production of interplanetary energetic electrons (Druge et al. 1989). This periodicity has been found not only in flare data but also in various indicators of solar activity such as the sunspot blocking function and the 10.7-cm flux from the whole Sun (Lean and Brueckner 1989).

After the discovery of the 154 day periodicity in the flare data of solar cycle 21, many people studied the periodicity in the activity data of cycle 20 (Bogart and Bai 1985; Ichimoto et al. 1985; Ozguc and Atac 1989). Although one finds a peak near 154 days in each power spectrum for cycle 20, in general, the peak near 154 days is weaker for cycle 20 than that for cycle 21. Lean and Brueckner (1989) analyzed various activity data for cycles 19 through 21. For cycle 21 they found a large peak near 158 days in the power spectra of the sunspot blocking function and the whole-Sun 10-cm radio flux. Similar results are obtained for cycle 20, but for cycle 19 a small peak near 159 days was found only in the spectrum of sunspot blocking function.

By analyzing the relationship between the 154-day periodicity and the distribution of flares on the Sun, Bai and Sturrock (1987) have shown the following. (a) This periodicity is not a local, but a global phenomenon.

Therefore, its mechanism must involve the whole Sun. (b) This periodicity is not due to the interaction of hot spots rotating at slightly different rates such that they overlap once every 154 days. (c) This periodicity is not caused by the interaction of "active bands," which are proposed (Wolff 1983) to be produced by g-mode oscillations of different l numbers.

Thus, the cause of the 154-day periodicity is still not understood. In order to gain insights on this problem, in the present paper we analyze the occurrence of energetic flares that produced interplanetary (IP) energetic protons, for cycles 19 through 21 (1955-86). In the same spirit, Kile, Cliver, and Fourgere (1990) analyze the occurrence rate of flares selected by 10-cm radio fluxes, for the same time interval. The preliminary results of these works have been reported by Bai, Cliver, and Kile (1990).

In Section II we discuss the event selection criteria. In Section III we discuss various methods of analyzing periodicity. In Section IV the results of our analyses are presented. In Section V we discuss and summarize the results.

## II. PROTON EVENT SELECTION: SOURCES AND PROCEDURE

# a) 1955-1969 Interval

For these years, we used the Catalog of Solar Particle Events 1955-1969 (Svestka and Simon 1975) as a data source. The proton events in this catalog are classified according to the three-digit classification system of Smart and Shea (1971) which is partially reproduced in Table 1. The first digit corresponds to the logarithm of the peak  $\geq$  10 MeV flux (protons cm<sup>-2</sup> s<sup>-1</sup> sr<sup>-1</sup>) measured by a near-Earth satellite. The second digit represents the 30 MHz absorption measured by a sunlit polar riometer, and the third digit

represents the response of a high latitude sea level neutron monitor. The classification system was constructed so that an event with a first digit of "1," for example, can be expected to also have second and third digits of "1." For our event list, we selected all events in the catalog with a first digit  $\geq 0$ , or, when satellite measurements were not available as indicated by a first digit of "X," we selected events with second or third digits > 0. In general, then, the threshold flux for our event selection corresponds to a peak flux of > 10 MeV protons ( $J(> 10 \text{ MeV})) \geq 1$  proton cm<sup>-2</sup> s<sup>-1</sup> sr<sup>-1</sup>, except for the period mainly before 1960, when less sensitive ground-based measurements were used and the effective threshold was  $J(>10 \text{ MeV}) \geq 10 \text{ proton cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1}$ .

Additional procedural details are as follows: (1) If the flare association for a proton event given in the catalog was characterized as "probable" or "certain," then the date of the flare was used for our list. If the flare association was only considered to be "possible," or if the responsible flare was thought to have occurred behind-the-limb and no flare time could be specified, then the date of the particle event onset was used. (2) If a proton event had both prompt and delayed (sudden-commencement (SC)) associated components, both of which exceeded the flux threshold, only the prompt component was considered. (3) Events attributed, at the "probable" or "certain" level, to recurrent geomagnetic storms were not included in our list; proton events with "possible" sources in recurrent storms were included. (4) An event on 1967 July 7 that exceeded the flux threshold (J>1 proton cm<sup>-2</sup> s<sup>-1</sup> sr<sup>-1</sup>), but was observed only by a *Pioneer* satellite located > 90° from the Earth-Sun line was omitted from our final list of events.

## b) 1970-1979 Interval

For these years, we used the Catalog of Solar Proton Events 1970-1979 (Akinyan et al. 1982) as a data source. As the name indicates, this catalog is a continuation of the Svestka and Simon (1975) catalog, and the Smart and Shea (1971) classification system was used here also. Thus, our selection criteria for these years were identical to those used for the period 1955-1969.

## c) 1980-1986 Interval

For these years, we used the Eighth Interplanetary Monitoring Platform (IMP-8) data on 20-40 MeV protons published in Solar-Geophysical Data (SGD). Assuming a "typical"  $E^{-3}$  energy spectrum (Van Hollebeke, Ma Sung, and McDonald, 1975), a proton event with a peak differential flux  $\geq 10^{-2}$  protons cm<sup>-2</sup> s<sup>-1</sup> sr<sup>-1</sup> MeV<sup>-1</sup> winhave an integral flux  $J(>10 \text{ MeV}) \geq 1$  proton cm<sup>-2</sup> s<sup>-1</sup> sr<sup>-1</sup>. Thus, all events with  $J(20-40 \text{ MeV}) \geq 10^{-2}$  above background were included in the list. To eliminate "modulation events" (see Section IId), we required a factor of five increase to identify a new event when an event was in progress, i.e., when  $J(20-40 \text{ MeV}) \geq 10^{-2}$ . Also, consistent with the procedure for 1955-1979, additional SC-related peaks were excluded. The SGD plots were supplemented by higher time resolution plots courtesy of R. E. McGuire for the years 1980-1983.

# d) Difficulties and Inconsistencies

The difficulties of compiling the list of proton events presented in the Svestka and Simon (1975) and Akinyan et al. (1982) catalogs are referred to in Akinyan et al. (p. 34).

There are many particle increases which show two or more components in their development. We consider them as two

or more new events only if the sources of the components was identified successfully [italics added]. Otherwise the particle flux increase was listed as one event.

This technique eliminates spurious events that may represent only a modulation of previously accelerated particles. Some real events may also be omitted, however. To supplement both of the above catalogs, we used a recent compilation by Shea and Smart (1989) of proton events from 1955-1986 with  $J(>10 \text{ MeV}) \ge 10 \text{ protons cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1}$  to make certain that no big events were left off our list. Eight events of a total of 385 were added in this manner.

For the years 1980-1986, we required  $J(> 10 \text{ MeV}) \ge 1 \text{ proton cm}^{-2} \text{ s}^{-1}$ sr-1 above background. This background subtraction was not done for the Svestka and Simon (1975) catalog. Akinyan et al. (1983) subtracted the background flux for isolated events and also for the initial component of compound events. Another source of inhomogeneity, mentioned above, in our final list of events involves the event selection threshold which is effectively higher for much of cycle 19 (before 1960) than for cycles 20 and 21. This higher effective threshold for the first half of cycle 19 is reflected in the number of events on our list from each solar cycle. For cycle 19 (nominally 1955-1964) we have 115 events, compared to 141 events for cycle 20 (1965-1975), and 129 events for cycle 21 through May 1986. The larger number of events in cycle 20 than in cycle 21 is mildly surprising, given the higher level of spottedness during cycle 21 (McKinnon 1987). The discrepancy may be due, at least in part, to our use of a single satellite for the years 1980-1986 (both the Svestka and Simon [1975] and Akinyan et al. [1983] catalogs considered multiple data sources) and the frequent gaps in IMP coverage during this period.

The dates of the proton flares we selected are listed in Table 2. As we have discussed above, proton-flare catalogs which we have used as data sources are based on observations by different detectors, and thus the event selection criteria we adopted are not exactly the same for the whole period. However, such changes are of much longer time scales than 154 days. Therefore, this does not influence the 154-day periodicity significantly.

#### III. METHODS OF PERIODICITY ANALYSIS

The standard method of periodicity analysis is the Fourier spectral analysis. The fast Fourier transformation (Cooley and Tukey 1965) is efficient and often used. The periodogram analysis (Scargle 1982) and the epoch folding method are also used. In the epoch folding method the period for which the phase diagram is the least uniform is searched for. In addition to these, the directionality analysis and the maximum likelihood method are used for periodicity analysis. In this section these latter two methods are discussed in more detail, because they are used in this paper and are perhaps less familiar to readers.

# a) Directionality (Rayleigh Power Spectrum) Analysis

Suppose we . It to determine whether n events with angular values of  $\{\theta_1, \theta_2, \theta_3, ..., \theta_n\}$  are uniformly distributed in angle. We can represent each event as a unit vector  $\mathbf{u}_i = \cos \theta_i \, \mathbf{e}_x + \sin \theta_i \, \mathbf{e}_y$ , where  $\mathbf{e}_x$  and  $\mathbf{e}_y$  are unit vectors parallel to the X-axis and Y-axis, respectively. The vector sum of these unit vectors is given by

$$U = \sum_{i=1}^{n} \cos \theta_i e_x + \sum_{i=1}^{n} \sin \theta_i e_y$$
 (1)

The magnitude of this vector divided by the number of events,

$$R = \frac{1}{1} \left\{ \left( \sum_{i=1}^{n} \cos \theta_{i} \right)^{2} + \left( \sum_{i=1}^{n} \sin \theta_{i} \right)^{2} \right\}^{\frac{1}{2}}, \tag{2}$$

indicates the uniformity of the distribution (Mardia 1972). If the events are uniformly distributed, R is very close to zero. If, on the other hand, the events are concentrated around a certain angle, R is close to 1. The direction angle of the vector  $\mathbf{U}$  shows the angle around which the events are concentrated. If we define the quantity, z, as

$$z = nR^{2} = \frac{1}{n} \left\{ \left( \sum_{i=1}^{n} \cos \theta_{i} \right)^{2} + \left( \sum_{i=1}^{n} \sin \theta_{i} \right)^{2} \right\}, \tag{3}$$

for randomly distributed events, the distribution of z follows P(z>K)=exp(-K) (Mardia 1972). We obtain the "Rayleigh power spectrum" z(v) by setting  $\theta_i=2\pi t_i/T=2\pi v_i$ , where  $\{t_i\}$  is a set of flare occurrence times and T is a variable period (Droge et al. 1989).

## b) Maximum Likelihood Method

Suppose the relative probability for flare occurrence is described by a sinusoidal distribution function,

$$P(t) = 1 + A \sin(2\pi t/T + \phi_0). \tag{4}$$

Here the mean probability is taken to be unity. Then, the joint pubbability of finding n flares with a set of occurrence times  $\{t_1, t_2, t_3, ..., t_n\}$  is given by

$$M(T, A, \phi_0) = \prod_{i=1}^{n} \left\{ 1 + A \sin \left( 2\pi t_i / T + \phi_0 \right) \right\}.$$
 (5)

This is a likelihood function. In the maximum likelihood method, we find the periodicity by finding the values of T, A, and  $\phi_0$  that maximize the

likelihood (e.g., Brandt 1976). If we take the logarithm of the above equation, we obtain a logarithmic likelihood function,

$$m(T, A, \phi_0) = \sum_{i=1}^{n} ln\{1 + A \sin(2\pi t_i/T + \phi_0)\}.$$

By determining the values of A and  $\phi_0$  that maximize the likelihood for various values of T, we can find the "likelihood power spectrum"  $m_m(T)$  as a function the period T only.

## c) Scargle's Periodogram

The periodogram is defined to be (Scargle 1982)

$$P_{x}(\omega) = \frac{1}{2} \left\{ \frac{\left[\sum_{i=1}^{N} X(t_{i}) \cos \omega (t_{i}-\tau)\right]^{2}}{\sum_{i=1}^{N} \cos^{2} \omega (t_{i}-\tau)} + \frac{\left[\sum_{i=1}^{N} X(t_{i}) \sin \omega (t_{i}-\tau)\right]^{2}}{\sum_{i=1}^{N} \sin^{2} \omega (t_{i}-\tau)} \right\}, \tag{7}$$

where  $X(t_i)$  is a time series (series of measurements arranged in order of time) for i=1, ..., N, and  $\tau$  is defined by the equation

$$\tan 2\omega \tau = \sum_{i=1}^{N} \sin 2\omega t_i / \sum_{i=1}^{N} \cos 2\omega t_i$$
.

# d) Comparison of the above Methods

Scargle's method has several advantages over the conventional fast Fourier transformation method (Horne and Baliunas 1986). First, it is convenient for analysis of unevenly sampled data. Second, for purely independently and normally (Gaussian) distributed noise with zero mean and constant variance  $\sigma$ , the power distribution follows an exponential distribution (Knight, Schatten, and Sturrock 1979; Scargle 1982; Horne and

Baliunas 1986); i.e., the probability of the power density at a given frequency being greater than K by chance is given by

$$P(z>K) = \exp(-K/\sigma^2) \tag{8}$$

The directionality analysis method and the maximum likelihood method can be used only when the measurements are counts of discrete events. When this is the case, we can show that Scargle's periodogram is equivalent to the Rayleigh power spectrum. For a large number of evenly sampled time series,

$$\sum_{i=1}^{N}\cos^{2}\omega\left(t_{i}-\tau\right)=\sum_{i=1}^{N}\sin^{2}\omega\left(t_{i}-\tau\right)=\frac{N}{2}.$$

If we substitute this expression into equation (7), it becomes identical to equation (3) except for the phase angle and the multiplication factor. However, equation (3) is independent of the choice of the X axis (phase angle). The Rayleigh power spectrum is simpler to calculate, when the total event number n is smaller than the number of time series N.

The maximum likelihood method is cumbersome, because we have to explore the phase space made of several parameters. However, this method has a couple of advantages over other methods. First, in this method, we have flexibility in the choice of the distribution function. Instead of a sinusoidal distribution function given by equation (4), we can use a step function, for example, if there is a good reason for it. Second, the logarithmic likelihood function is cumulative. We will make use of this in the next section.

By applying the above three methods and the Fourier spectral analysis to the same set of data, we have confirmed that they all give almost identical results, except for normalization. If we use the sinusoidal probability given by equation (4), the likelihood function as a function of period (or frequency) turns out to be similar to the Rayleigh power spectrum not only in shape but also in magnitude. As we discussed earlier, the Rayleigh power spectrum is supposed to be normalized, when the occurrences of all events are independent. We have confirmed this by Monte Carlo simulations. However, the occurrences of proton flares are not independent, because some active regions produce more than one proton flare. Owing to this, as we shall see in the next section, the Rayleigh power spectrum is not normalized. Droge et al. (1989) did not take this effect into account in estimating the statistical significance of the 154-day periodicity of "electron flares."

Even if we use a normalized time series,

$$X_{i} = (X_{i} - X_{av})/\sigma,$$

where  $X_i$  is the number of proton tlares on the ith day,  $X_{av}$  is the average daily proton flare number, and  $\sigma$  is the variance, because of the interdependence of occurrences of some proton flares, the Scargle's periodogram turns out to be not normalized. Therefore, whatever analysis method is used, the best way to normalize the power spectrum is to fit the actual power distribution to equation (8).

#### IV. ANALYSIS

# a) Solar Cycle 21

Because the 154-day periodicity was initially found in the activity data of solar cycle 21, we first discuss the results for cycle 21. Figure 1 shows the normalized power spectrum of the occurrence rate of proton flares for cycle

21 (a) and that for the time interval from 1978 February 15 to 1983 August 6 (b). The 154-day periodicity is found to be operative mainly in the latter interval during cycle 21, as shown below. For this figure power spectra were calculated for the 31-230 nHz (50-373 days) range with 1 nHz intervals.

Figure 2 shows the distribution of the Rayleigh power values corresponding to the normalized spectrum shown in Figure 1b. The vertical axis shows the cumulative number of frequencies for which the Rayleigh power exceeds a certain value. Of course, for all 200 frequencies the Rayleigh power exceeds 0; thus, we have a point at (X=0, Y=200). At only one frequency (75 nHz, which is equivalent to 154.3 days) the Rayleigh power was 14.2, its maximum value. For lower values of Rayleigh power, the distribution can be well fit by the equation Y = 200 exp(-X/1.70), as expected from equation (8). Thus, we normalize the power spectrum by dividing the Rayleigh powers by 1.70 to obtain Figure 1b. For other cases, we use the same procedure for normalization.

In estimating the statistical significance of the peaks in the power spectrum, the "faise alarm probability" may be used. It is given by the expression,

$$F = 1 - [1 - exp(-z_m)]^N, (9)$$

where  $z_m$  is the height of the peak in the normalized power spectrum and N is the number of independent frequencies (Scargle 1982; Horne and Baliunas 1986). The interpretation of F is as follows. If we have a discrete power spectrum giving the power at each of N independent frequencies for a set of random data, F indicates the probability that the power at one or more of these frequencies will exceed  $z_m$  by chance. The number of independent frequencies is determined by  $N=(f_1-f_2)/\Delta f_{ifs}$ . Here  $f_1-f_2$ , is the

frequency range, and the independent Fourier spacing is given by  $\Delta f_{ifs}=1/\tau$ , where  $\tau$  is the time span of the data.

For  $\tau=5.5$  years = 2008 days,  $\Delta f_{ifs}=5.8$  nHz. Thus, there are 34 independent frequencies in the 31-230 nHz interval. We over sampled to obtain the power spectrum shown in Figure 1b, in which the height of the peak at 154.3 days is 8.36. The over sampling tends to increase the peak value. Therefore, if we substitute  $z_m$ =8.36 and N=34 into equation (9), we underestimate the false alarm probability. However, if we substitute N=200(since we searched 200 frequencies with 1 nHz intervals) into equation (9), it turns out that it adequately compensates the effect of increase of the peak value by over sampling. By using  $z_m=8.36$  and N=200, we get F=0.046. Because we searched for the time interval which maximizes the value of the 154-day peak, we must include the effect of this search in estimating the false alarm probability. Even if the data set is random, we can increase the peak power somewhat by interval searching. By Monte Carlo simulations, we find that the effect is a reduction in the flase alarm probability by about 3. Therefore, we can conclude that the probability of obtaining by chance such a high peak as in Figure 1b in the 50-370 day interval is about 14%.

For the sake of comparison, we list in Table 3 the peak values of the normalized power for different data sets for cycle 21. For the case of HXRBS flares, we used flares with peak count rates > 1000 counts s<sup>-1</sup> only. We used a uniform procedure to obtain the results. The peak value for proton flares is comparable to those for HXRBS flares and GRS flares but considerably smaller than that for electron flares. Since the proton flare occurrence rate conforms to the 154-day periodicity found from other data sets, it is reasonable to use the proton data to study the flare activity periodicity for earlier times.

In order to determine the time interval in which the 154-day periodicity was operative, we have used the fact that the logarithmic likelihood function is cumulative. We define m(k) as follows:

$$m(k) = \sum_{i=257}^{k} ln\{1 + 0.45 \sin \left[2\pi (t_i - 8524)/154d + 0.5\pi\right]\}.$$
 (10)

Here we use T=154 d somewhat arbitrarily, and the phase and amplitude of the sinusoidal function are chosen to maximize the likelihood for k=385. (The 257th event since 1955 is the first event of cycle 21, and the 385th is the last.) If events occur at random phases, the value of  $y=1+A\sin(2\pi t/T+\phi_0)$  is 1 on the average, and thus the value of  $\ln y=\ln (1+A\sin(2\pi t/T+\phi_0))$  is zero on the average. However, if event occurrences conform to the periodicity, more events occur when the value of  $y=1+A\sin(2\pi t/T+\phi_0)$  is bigger than 1. Thus, for time intervals when the preton flare occurrence rate conforms to the periodicity, m(k) increases on the average as k increases; for time intervals when it does not conform to the periodicity, m(k) fluctuates or decreases as k increases. Therefore, equation (10) provides a good way of determining when the periodicity is operative. In Figure 3 we find that m(k) increases on the average for the interval between event numbers 270 and 370.

Figure 4 shows the flare occurrence rate as a f nction of time for the time interval from 1977 September 14 through 1984 November 9 (which includes events with event numbers 270-370). For this figure the occurrence rate has been smoothed with a triangular window function having a total duration of 61 days. The 154-day periodic modulation of the flare occurrence rate is semi-regular in the time interval from about 1978 February 15 to 1983 August 6. By analyzing the occurrence rate of the proton flares for this

epoch only, we find that the best determined period is 153.7±1.5 days (one sigma error). Hence, the vertical grid lines have been placed 153.7 days apart, and they are positioned such that the maximum phases of the periodicity fall in the middle of grid lines. This epoch corresponds to 13 cycles. The time of first maximum of the 154-day periodicity in this epoch is 1978 May 3 (t=8524 days since 1955 January 1), which is indicated by an arrow in Figure 4. SMM observations have shown that the 154-day periodicity repeated 8 cycles during the 1980-83 interval (Rieger et al. 1984; Dennis 1985). The present result extends the epoch for 154-day periodicity further back in time in cycle 21.

The 218-day peak in Figure 1a is comparable to the 154-day peak. However, interval searching described above does not increase the 218-day power appreciably. Inspection of the proton occurrence time profiles shows that the power for the 218 day peak is mainly contributed by four episodes (around t=8525, 9598, 10058, and 11357 days) of strong flare activity, which are separated by approximately integer multiples of 218 days. Therefore, we do not regard the 218-day periodicity statistically significant.

# b) Solar Cycles 19 and 20

The power spectrum for cycles 19 and 20 combined is shown in Figure 5a. Using the analysis described above, the 154 day periodicity is found to be operative mainly in the interval from the beginning of 1958 to the end of 1971, and the power spectrum for this interval is shown in Figure 5b. The normalized height of the 154-day peak is 7.62 for Figure 5a and 11.68 for Figure 5b. The false alarm probability of obtaining by chance a peak with  $z_m$ =11.68 in the 31-230 nHz (50-370 days) interval by chance is only 0.2%. The probability of obtaining such a high peak in the neighborhood of 154 days by

chance is considerably smaller (of order of 10<sup>-5</sup>). If we perform the spectral analysis for cycle 19 and cycle 20 separately, the normalized heights of the 154-day peaks are 3.0 and 5.5, respectively. Because the epoch for the 154-day periodicity is stretched over a part of cycle 19 and a part of cycle 20, he 154-day peaks for individual cycles become statistically insignificant.

Figure 6 shows the proton flare occurrence rate as a function of time for the interval from 1958 January 1 through 1972 May 22. The occurrence rate has been smoothed with a triangular window function having a total duration of 61 days. The proton flare occurrence rate shows a semi-regular 154-day periodic for the 14-year time interval from 1958 through 1971 (except for few cycles). This interval corresponds to 33 cycles. (In comparison, the 11-year solar cycle, admittedly a more regular phenomenon, is in its 27th repetition after the Maunder minimum.) The best-determined period for this epoch is 154.6±0.6 days (one sigma error); hence the vertical grid lines are 154.6 days apart. From the phase angle calculation, we find that the time of the first maximum of the 154-day periodicity in this epoch is 1958 March 25 (t=1180 days since 1955 January 1), which is indicated by an arrow in Figure 6.

# c) Phase shift

We have found that the 154-day periodicity is operative mainly in two epochs: from 1958 January to 1971 December and from 1978 February to 1983 August. Figure 7 shows the annual number of proton flares for the 32 years from 1955 through 1986. The two epochs for the 154-day periodicity are shown with horizontal lines. Because the first epoch covers the maxima of two solar cycles, we can infer that the 154-day periodicity is not a phenomenon subordinate to the 11-year cycle.

The best-determined period is 154.6±0.6 days for the first epoch and 153.7±1.5 days for the second epoch, and they are in agreement within the errors. Now let us study the phase relationship between the 154-day periodicity in these two epochs. The time of the first maximum of the periodicity in the first epoch is 1180 days, and that for the second epoch is 8524 days. We find that the time interval between them is 47.5 times 154.6 days; i.e., 8524-1180=154.6x47.5. Thus, we find that a phase shift of about 0.5 (180°) has occurred to the periodicity between the two epochs. Considering the uncertainty of the period 154.6±0.6 days, the phase shift is between 0.32 and 0.69.

We can calculate the phase shift, by calculating the Rayleigh power after adding a variable time shift  $\Delta t$  to the occurrence times of the proton flares of cycle 21. Then, the Rayleigh power near 154 days is a function of both period and time shift. We have found that the Rayleigh power attains the maximum value when the period T=154.6 days and  $\Delta t$ =77 days. Thus, the 154.6-day periodicity of cycle 21 is phase-shifted by about 0.5 ( $\Delta \phi$ =77/154.6=0.5) with respect to that of the earlier epoch. The black dot in Figure 8 indicates the location where the Rayleigh power attains the maximum, and the contour line shows a 1- $\sigma$  range. (In estimating the 1- $\sigma$  range, we have taken into account the proper normalization of the power spectrum.) Thus, T=154.6(±0.6) days, and  $\Delta \phi$ =0.5±0.16. This result agrees with the above result from the straightforward method. Our analysis shows that the hypothesis of a phase shift of 0.5 is 73 times more likely than the hypothesis of no phase shift.

Figure 9 shows the phase diagrams for the above-mentioned two epochs when the 154.6-day periodicity was operative. We find that the amplitudes of the modulation of the flare rate are large; it changes by a

factor of 6 from peak to valley. We also find a phase shift of about 0.5 between the two phase diagrams, in agreement with Figure 8. Bogart and Bai (1985) claimed that the phase of the 154-day periodicity remained coherent from cycle 20 to cycle 21. However, because the uncertainty of the period is large for their result (about 2 days), the phase coherency cannot be determined. The uncertainty of the period is only 0.6 days for the present result because of the long duration of the first epoch for the 154-day periodicity, and thus we can study the phase shift meaningfully.

For comparison with Figures 4 and 6, in Figure 10 we plot the proton flare occurrence rate for the interval from the beginning of 1972 through the end of 1977. According to the above discussions, the proton flare occurrence in this interval does not conform to the 154.6-day periodicity. The power spectrum for this interval is found not to have any statistically significant peaks.

#### V. DISCUSSION

## a) Comparison with Other Results

The 154-day periodicity found in the proton flare occurrence rate of cycle 21 is consistent with the results from other data sets. Initially this periodicity was found to repeat 8 cycles during 1980-83. Whether this periodicity commenced before 1980 cannot be answered by analyzing SMM observations, which began in 1980 February. From the time profile of microwave flares (Fig. 1 of Bogart and Bai 1985), we find that this periodicity began to operate in 1980 for microwave flares. The present study, however, shows that the 154-day periodicity was operative since 1978 February for 13 or 14 cycles.

The 154-day periodicity of the proton flare occurrence was semi-regular in the interval from the beginning of 1958 to the end of 1971 during cycles 19 and 20. The 154-day peak is statistically significant for this interval. However, 154-day peak becomes statistically insignificant, if we calculate the power spectra of proton flares for cycles 19 and 20 separately. This is because the epoch for the 154-day periodicity is stretched over the two solar cycles. This may be one of the reasons why the 154-day periodicity is not very significant in the power spectra of other data sets analyzed for cycle 20 alone.

While the 154-day periodicity is significant in the proton flare occurrence rate for the 1958-71 interval, the occurrence rate of flares selected by the 10-cm radio fluxes does not show any significant periodicity near 154 days in the same interval nor in cycle 20 (Kile, Cliver, and Fougere 1990). It is probable that the 154-day periodicity influences the occurrence rates of different types of flares differently.

Bai (1987) discovered a 51-day periodicity in the occurrence rate of major flares for cycle 19. The major flares in this study are flares with comprehensive flare indices (CFIs) greater than 5, which were selected from the compilations of Dodson and Hedeman (1971, 1975). Similarly, Kile, Cliver, and Fougere (1990) found a 51-day peak (at a less significant level) in the power spectrum of the occurrence rate of microwave (2.8 GHz) flares for this cycle. However, we do not find any statistically significant periodicity near 51 days in the proton flare rate of cycle 19 nor of any other cycles. Lean and Brueckner (1989) also did not find the 51-day periodicity in the power spectra for solar cycle 19. It is not clear why the proton flare rate, at least from 1958, and the sunspot blocking function exhibit the 154-day periodicity

during cycle 19, while the occurrence rate of flares selected by CFIs and microwave fluxes exhibit the 51-day periodicity during cycle 19.

Table 4 summarizes results of periodicity analyses by various authors using different observations. We see that the evidence of the 154-day periodicity has been found in several data sets for at least parts of cycles 19, 20, and 21. We also see that the 51 day periodicity has been found in two data sets for cycle 19. The 154-day periodicity could be regarded as a subharmonic of the 51-day periodicity. The 51-day periodicity has also been detected in the solar diameter measurements (Delache, Laclare, and Sadsaoud 1985).

From the above discussions, it appears that the occurrence rate of proton flares is more sensitive to the 154-day periodicity than flares selected by other criteria. This conclusion is based on the results of cycles 19 and 20 discussed above, in particular, the absence of evidence for the 154-day periodicity in the 10-cm burst and CFI data for the 1958-1971 epoch (Kile, Cliver, and Fourgere 1990). During cycle 21, the 154 day periodicity became operative since 1978 February in the proton flare occurrence rate, while it became apparent only after 1980 in the occurrence rate of flares selected by microwave emission.

## b) Intermittence and Phase Shift

Perhaps the most important result of this work is that the 154-day periodicity is intermittent by showing up in two different epochs, and that the phase has changed by about 0.5 from one epoch to the next. Simple analogies may help illucidate the physical meaning of this finding. A damped linear oscillator can exhibit intermittence and a phase shift. When a damped linear oscillator is excited, it shows a periodic modulation with a

certain amplitude. As time goes on, its amplitude decays, and when the amplitude is comparable to the noise, the periodic modulation is no longer discernible. After another excitation of the oscillator, it again shows a periodic modulation. However, the later excitation is not necessarily in phase with the earlier periodic modulation.

The analogy to a damped linear oscillator, however, is not consistent with observations in the following aspects. First, we do not see any obvious sign of the monotonic decay of the amplitude in the flare rate shown in Figures 4 and 6. Also we see linear increases of the logarithmic likelihood with increasing event number in Figure 3. Second, the proton flare rate began to show the 154-day periodicity from 1978 February during cycle 21, but the rate of microwave flares began to show the periodicity only after 1980 January. Therefore, if anything, the periodicity was stronger (or more influential) during the 1980-83 interval than 1978-79 interval.

We can think of another analogy. A damped nonlinear oscillator with a periodic forcing term can show periodic behavior sometimes and chaotic behavior at other times. For example, the damped, periodically forced nonlinear oscillator described by so-called Duffing's equation,

$$\frac{d^2x}{dt^2} + k\frac{dx}{dt} + x^3 = B \cos t, \tag{11}$$

shows periodic behavior for certain values of parameters k and B, and chaotic behavior for slightly different values (Thompson and Stewart 1986). This oscillator can show an order 3 subharmonic periodicity as well as the fundamental periodicity. It is interesting to note that the 154-day periodicity can be interpreted as the order 3 subharmonic of the 51-day periodicity.

We wish to thank J. A. Klimchuk and J. N. Kile for helpful discussions and critical reading of the manuscript. Comments by an anonymous referee were helpful. The work at Stanford was supported by Office of Naval Research Contract N00014-85-K-0111, by NASA grant NGL 05-020-272, and as part of the Solar-A collaboration under NASA contract NASA 8-37334 with Lockheed Palo Alto Research Laboratories.

Table 1
Solar Proton Event Classification System (Smart and Shea 1971)

Digit	First	Second	Third		
	>10 MeV proton flux (protons cm <sup>-2</sup> s <sup>-1</sup> sr <sup>-1</sup>	Daylight polar cap absorption at 30 MHz	Sea level neutron monitor increase (%)		
0	100 - <101	No measurable increase	No measurable increase		
1	101 - < 102	<1.5	<3		
2	100 - <101	1.5 - <4.6	3 - <10		
X	Measurement not available				

TABLE 2
DATES OF PROTON FLARES

No.	Dates		No.	1	Dates No. Dates				No	Datas				
					Date:	· · · · ·						Dates		
1	55 Jan		48		Aug		95			12	142		Nov	2
2	56 Feb		49	58	Aug		96			15	143	67	Nov	
3	56 Mar		50	58	Sep		97	61		18	144	67	Nov	
4	50 Apr		51	59	Jan		98	61		20	145	67	Nov	
5	56 Aug		52	59		12	99	61		24	146	67	Dec	3
6 7	56 Nov 57 Jan		53 54	59 59	May		100 101	61 61	Sep	7	147	67	Dec	
8		20 21	5 <del>4</del> 55	59	Jun Jun	9 12	101	61		10 28	148 149	67	Dec	
9	57 Apr	3	56	59	Jul	10	103		_	10	150	67 67	Dec	
10	57 Apr	6	57	59	Jul	14	104		Feb	1	151	67	Dec Dec	18
11	-	11	58	59	Jul	16	105		Feb	4	152	68	Jan	
12	•	17	59	59		18	106			20	153	68	Jan	
13	57 May	8	60	59	Aug		107			23	154		Feb	8
14	_	19	61	59	Sep	1	108	63		15	155	68	Feb	
15	-	19	62	60	Jan		109	63	Aug	6	156	68	Apr	26
16		22	63	60	Mar	30	110	63	Aug	9	157	68	Jun	9
17	57 Jun	30	64	60	Mar	30	111	63		15	158	68	Jul	6
18	57 Jul	3	65	60	Apr	1	112	63		16	159	68	Jul	8
19	57 Jul	24	66	60	Apr	5	113	63	Sep 2	20	160	68	Jul	12
20	57 Jul	28	67	60	Apr	28	114	63	Sep 2	26	161	68	Jul	12
21	57 Aug	9	68	60	Apr	29	115	64	Apr :	16	162	68	Sep	26
22	•	27	69	60	May	4	116		Feb	5	163	68	Sep	28
23	-	28	70	60	May	6	117	65		4	164	68	Sep	29
24		29	71	60	May	9	118	66		24	165	68	Oct	3
25	57 Aug		72	60	May		119		May	2	166	68	Oct	23
26	57 Sep	2	73	60	May	17	120	66	Jul	7	167		Oct	29
27	57 Sep		74	60	May		121	66	Jul	9	168		Oct	30
28	57 Sep		75	60	Jun	1	122	66		28	169		Oct	30
29	57 Sep		76	60	Jun		123	66	Sep	2	170		Nov	1
30	57 Sep		77	60	Jun		124	υ6	Sep	4	171		Nov	4
31		20	78	60	Aug		125	66	Sep	4	172		Nov	18
32 33		16	79	60	Aug		126	66	-	14	173		Nov	20
34		16 28	80 81	60	_	26	127 128	66 67	•	14 28	174		Nov	21
35	58 Feb	9	82	60 60	Sep	3	129	67		28 28	175 176		Dec Jan	2
36	58 Mar		83		Sep Oct		130		Feb		177		Jan	
37	58 Mar		84		Oct		131		Feb		178		Feb	
38	58 Mar		85		Nov		132	67			179		Feb	
39	58 Mar		86		Nov		133	67	May		180		Feb	
40	58 Mar		87		Nov		134	67			181		Feb	
41	58 Apr		88		Nov		135	67		3	182		Mar	
42	58 Jun	4	89		Nov		136	67	Jun	6	183		Mar	
43	58 Jun	6	90		Nov		137	67			184			
44	58 Jul	7	91		Nov		138	67	Aug	1	185		Mar	
45	58 Jul		92		Dec	5	139	67	_	3	186		Apr	
46	58 Aug		93		Apr		140	67		4	187		Apr	
47	58 Aug	19	94	61			141		Aug	9	188		May	

No. Dates	No. Dates	No. Dates	No. Dates
189 69 Jun 7	239 72 Oct 29	288 78 Oct 8	337 81 Dec 27
190 69 Sep 25	240 72 Nov 2	289 78 Oct 9	338 82 Jan 2
191 69 Oct 14	241 73 Apr 11	2_0 78 Oct 17	339 82 Jan 30
192 69 Oct 14	242 73 Apr 29	291 78 Nov 10	340 82 Feb 1
193 69 Nov 2	243 73 Jul 29	292 78 Dec 11	34: 62 Feb 8
194 69 Nov 7	244 73 Sep 7	293 79 Feb 16	342 82 Mar 7
195 69 Nov 24	245 74 Jul 2	294 79 Mar 1	343 82 Mar 30
196 69 Dec 18	246 74 Jul 4	295 79 <b>Mar</b> 9	344 82 Jun 3
197 69 Dec 20	247 74 Jul 5	296 79 Apr 3	345 82 Jun 27
198 69 Dec 30	248 74 Jul 6	297 79 Jun 5	346 82 Jul 9
199 70 Jan 29	249 74 Sep 10	298 79 Jul 5	347 82 Jul 12
200 70 Jan 31	250 74 Sep 12	299 79 Aug 3	348 82 Jul 19
201 70 Mar 6	251 74 Sep 19	300 79 Aug 17	349 82 Jul 22
202 70 Mar 7	252 74 Sep 23	301 79 Aug 21	350 82 Aug 14
203 70 Mar 23	253 74 Nov 5	302 79 Sep 8	351 82 Sep 4
204 70 Mar 25	254 75 Aug 3	303 79 Sep 14	352 82 Nov 22 353 82 Nov 26
205 70 Mar 29	255 75 Aug 21 256 75 Aug 22	304 75 Nov 15 305 79 Nov 21	<del>-</del>
206 70 May 30 207 70 Jun 25	256 75 Aug 22 257 76 Mar 23	=	354 82 Dec 7 355 82 Dec 14
	258 76 Mar 29	306 80 Feb 6 307 80 Apr 4	356 82 Dec 17
	259 76 Apr 30	308 s0 Jul 5	357 82 Dec 19
	260 76 Aug 22	309 80 Jul 17	358 82 Dec 25
210 70 Aug 11 211 70 Nov 5	261 77 Sep 7	310 80 Aug 6	359 82 Dec 26
212 70 Dec 11	262 77 Sep 9	311 80 Oct 15	360 83 Jan 6
212 70 Dec 11 213 70 Dec 24	263 77 Sep 16	312 80 Nov 14	361 83 Feb 3
214 71 Jan 24	264 77 Sep 19	313 80 Nov 23	362 83 Mar 10
215 71 Apr 1	265 77 Sep 24	314 81 Mar 7	363 83 Apr 15
216 71 Apr 6	266 77 Oct 12	315 81 Mar 25	364 83 Jun 14
217 71 Apr 20	267 77 Nov 22	316 81 Mar 30	365 84 Jan 31
218 71 Apr 22	268 77 Dec 27	317 81 Apr 1	366 84 Feb 16
219 71 May 16	269 78 Jan 1	318 81 Apr 3	367 84 Feb 17
220 71 Sep 1	270 78 Jan 8	319 81 Apr 10	368 84 Mar 7
221 71 Oct 3	271 78 Feb 13	320 81 Apr 14	369 84 Mar 10
222 71 Dec 14	272 78 Feb 25	321 81 Apr 24	370 84 Mar 14
223 72 Jan 10	273 78 Apr 8	322 81 Apr 28	371 84 Apr 24
224 72 Jan 20	274 78 Apr 11	323 81 Apr 30	372 84 May 22
225 72 Mar 5	275 78 Apr 16	324 81 May 4	373 84 May 31
226 72 Apr 17	276 78 Apr 19	325 81 May 8	374 85 Jan 21
227 72 Apr 18	277 78 Apr 21	326 81 May 10	375 85 Apr 24
228 72 May 28	278 78 Apr 28	327 81 May 16	376 85 Jul 2
229 72 Jun 8	279 78 Apr 29 280 78 Apr 30	328 81 Jul 20 329 81 Jul 24	377 85 Jul 9 378 85 Jul 17
230 72 Jun 16			378 85 Jul 17 379 86 Feb 4
231 72 Jul 19	281 78 May 7 282 78 May 11	330 81 Aug 7 331 81 Sep 17	380 86 Feb 6
232 72 Jul 22 233 72 Jul 23	283 78 May 31	331 Al Sep 17	381 86 Feb 7
	284 78 Jun 22	333 81 Oct 12	382 86 Feb 10
	285 78 Jul 10	334 81 Nov 14	383 86 Feb 14
235 72 Aug 4 236 72 Aug 7	286 78 Sep 7	335 81 Dec 5	384 86 Mar 6
236 72 Aug 11	287 78 Sep 23	336 81 Dec 9	385 86 May 4
237 72 Aug 11 238 72 Aug 16	201 10 OCP 20	330 01 200 3	202 00 1241 .
230 12 Aug 10			

TABLE 3
NORMALIZED PEAK VALUES NEAR 154 DAYS

Data	Time interval	Peak Frequency	Normalized Peak value	
Proton flares	78 Feb - 83 Aug	75 nHz	8.36	this work
Electron flares	78 Aug - 82 Dec	76 nHz	12.83	Droge et al. (1990)
HXRBS flares	80 Feb - 83 Dec	75 nHz	7.44	Dennis et al. (1985)
GRS flares	80 Feb - 83 Dec	75 nHz	8.87	Vestrand et al. (1987)

Table 4
OBSERVATIONS OF 154-DAY PERIODICITY<sup>1</sup>

		Cycle		
Observed Activity	19	20	21	References <sup>2</sup>
Gamma-ray Flares			Y	a
GOES Soft X-ray Flares			Y	a
HXRBS Flares			Y	b
Microwave Flares		ү3	Y	c
H-alpha Flares		<b>Y</b> 3	Y	d
Flare Index		<b>y</b> 3	Y	e
Sunspot Area	<b>Y</b> 3	Y	Y	f
Quiet Sun10-cm Radio Flux	N	Y	Y	f
Flares with I.P. Electrons			Y	g
Flares with I.P. Protons	Y	Y	Y	h
Flares selected by C.F.I.	5 <u>1</u> d	N		h, i, j
Flares selected by 10-cm Flux	51d	N	Y	j

#### **Notes**

- 1. The letter "Y" means yes, and "N" means no. Blank areas indicate either no measurements or no analyses. During cycle 20, the occurrence rates of flares selected by CFIs and by10-cm radio fluxes do not exhibit a154-day periodicity.
- 2. Reference code: a- Rieger et al. (1984); b-Kiplinger et al. (1984); c-Bogart and Bai (1985); d-Ichimoto et al. (1985); e-Özgüc and Ataç (1989); f-Lean and Brueckner (1989); g-Dröge et al. (1989); h-Present paper; i-Bai (1987); j-Kile, Cliver, and Fougere (1990).
- 3. The statistical significance is low for these cases.

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## FIGURE CAPTIONS

- Fig. 1--Normalized power spectra of the proton flare occurrence rate.
- Fig. 2--Rayleigh power distribution. The vertical axis is the number of frequencies for which the Rayleigh power exceeds X. The straight line is the fit to the points for lower values of Rayleigh power.
- Fig. 3--The logarithimic likelihood function as a function of the last event number (see eq. 10 for the definition). Notice that the logarithmic likelihood function increases almost linearly between events 270 and 370. The momentary decrease of the likelihood in the interval for event numbers between 325 and 340 is due to the two misbehaving 154-day cycles around t=9830 days (see Fig. 4).
- Fig. 4--Smoothed occurrence rate of proton flares for the interval between 1977 September 14 and 1984 November 9. The periodic modulation is semi-regular for 13 cycles from 1978 February 8 through 1983 August 6, except for two cycles around day 9830.
- Fig. 5--Normalized power spectra of the proton flare occuurrence rate.
- Fig. 6--Smoothed occurrence rate of proton flares for the interval from 1958 Jan 1 to 1972 May 22. The positions of vertical grid lines, which are 154.6 days apart, are chosen such that the peak phase falls near the mid points. Notice that the 154.6-day periodicity is semi-regular for 33 consecutive cycles, with only a few irregular cycles.
- Fig. 7--Yearly number of proton flares. The two epochs when the 154-day periodicity was operative are shown by two horizontal lines in the upper part of the figure. The occurrence rate shows a dip near the maximum of cycle 19 and also near the maximum of cycle 21.

Fig. 8--Phase diagrams for the two epochs when the 154-day periodicity was in operation. Notice large amplitudes of modulation and a phase shift of about 0.5. The beginning of 1955 is chosen as the zero phase.

Fig. 9--Time shift between the 154-day periodicity of the two epochs. The solid dot indicates the location (T=154.6 days,  $\Delta t$ =77 days) where the power is the strongest. The contour line indicates the parameter range of one standard deviation

Fig. 10--Smoothed occurrence rate of proton flares for the interval from the beginning of 1972 to the end of 1977. Vertical grid lines are 154.6 days apart. During this interval, the proton flare rate shows no periodic modulation.

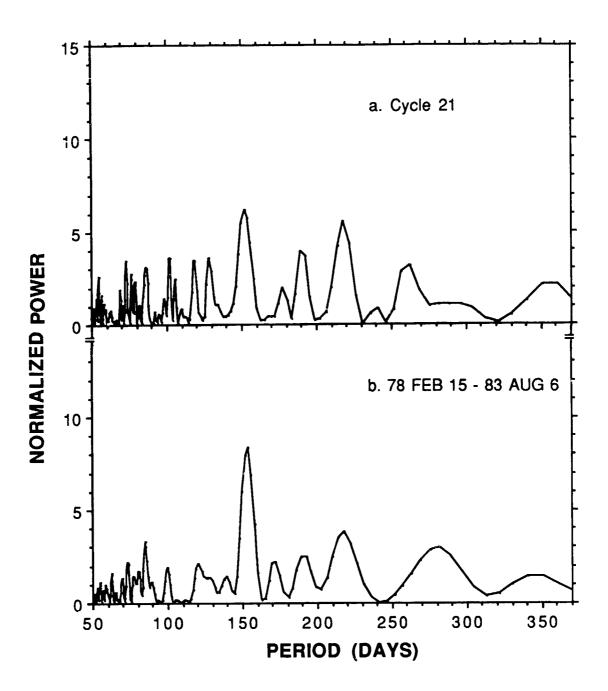


Fig. 1

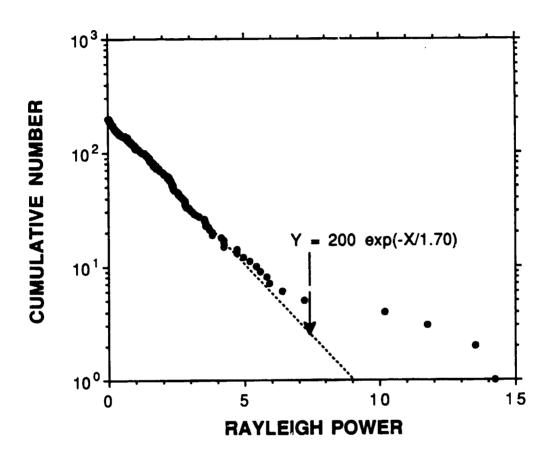


Fig. 2

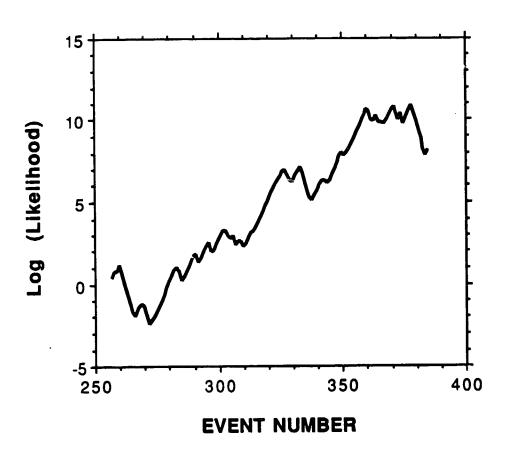


Fig. 3

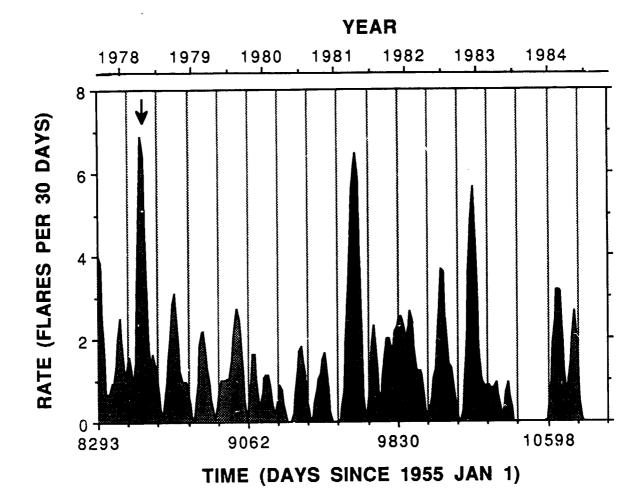


Fig. 4

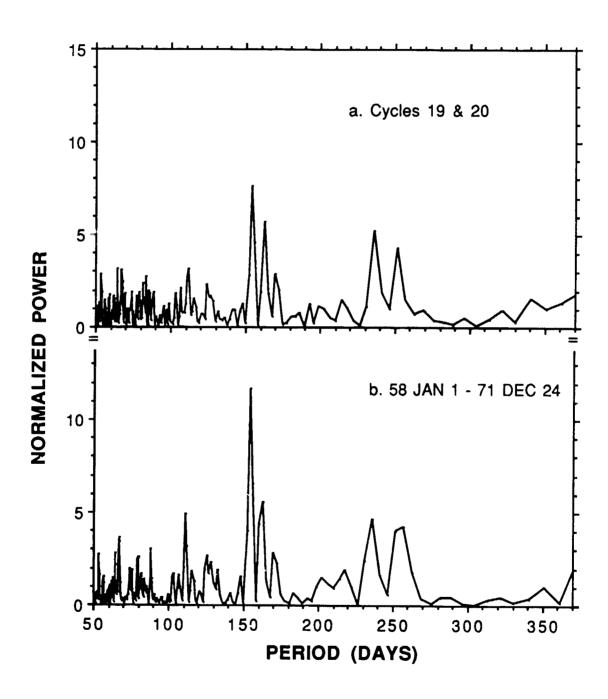
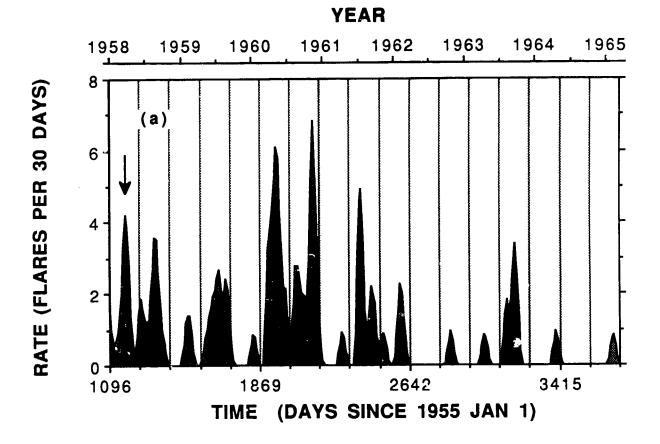


Fig. 5



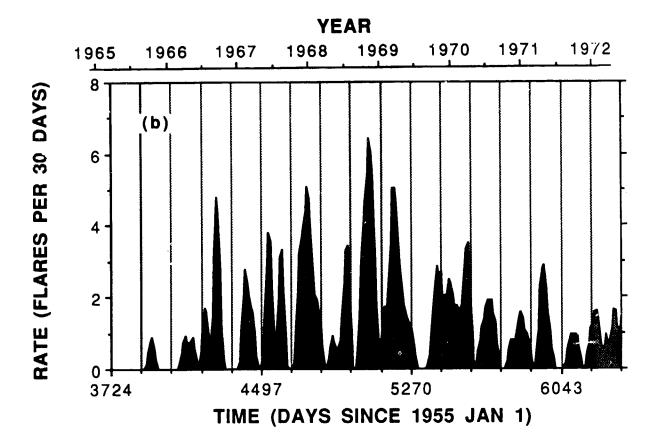


Fig. 6

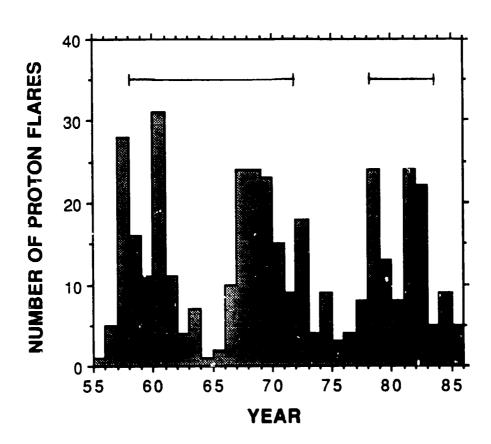


Fig. 7

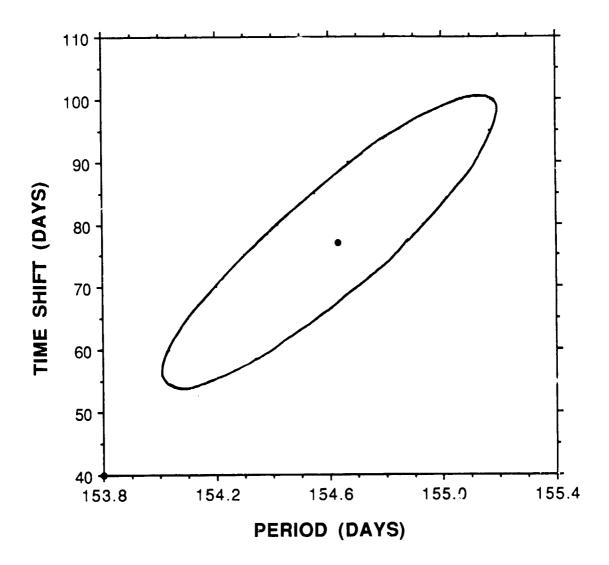


Fig. 8

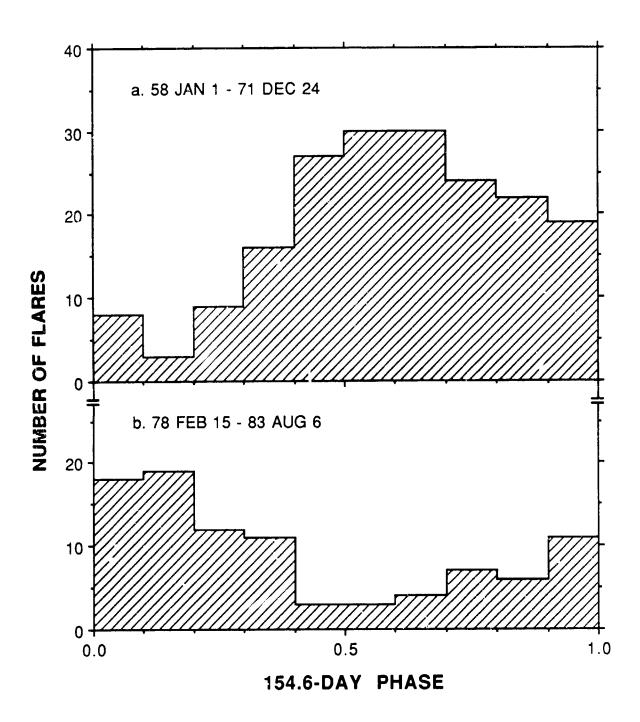


Fig. 9

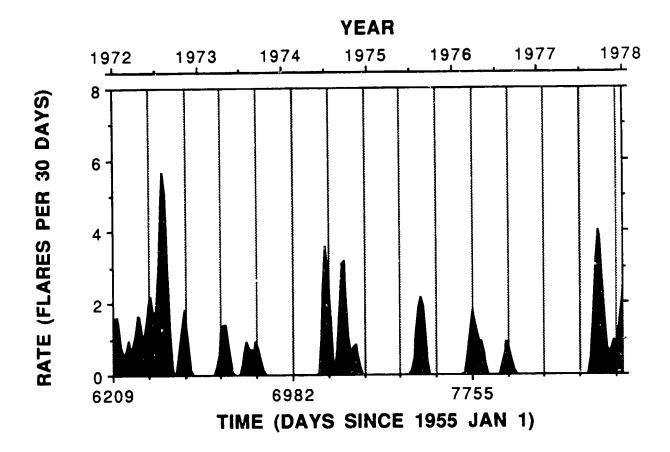


Fig. 10